# Decision Making Theory 

Week 7
Assignment Method

## Assignment Method

$\square$ A special class of linear programming models that assign tasks or jobs to resources
$\square$ Only one job (or worker) is assigned to one machine (or project)

## MINIMIZATION

## Example

## $\nabla$ Build a table of costs or time associated with particular assignments

|  | Typesetter |  |  |
| :--- | :---: | :---: | :---: |
| Job | A | B | C |
| R-34 | $\$ 11$ | $\$ 14$ | $\$ 6$ |
| S-66 | $\$ 8$ | $\$ 10$ | $\$ 11$ |
| T-50 | $\$ 9$ | $\$ 12$ | $\$ 7$ |

## Step 1

| Typesetter | A | B | C |
| :--- | :---: | :---: | :---: |
| Job |  |  |  |
| R-34 | $\$ 11$ | $\$ 14$ | $\$ 6$ |
| S-66 | $\$ 8$ | $\$ 10$ | $\$ 11$ |
| T-50 | $\$ 9$ | $\$ 12$ | $\$ 7$ |

Step 1a - Rows
Step 1b-Columns

| Typesetter | A | B | C |
| :--- | :---: | :---: | :---: |
| R-34 | $\$ 5$ | $\$ 8$ | $\$ 0$ |
| S-66 | $\$ 0$ | $\$ 2$ | $\$ 3$ |
| T-50 | $\$ 2$ | $\$ 5$ | $\$ 0$ |


| Typesetter | A | B | C |
| :--- | :--- | :--- | :--- |
| Job |  |  |  |
| R-34 | $\$ 5$ | $\$ 6$ | $\$ 0$ |
| S-66 | $\$ 0$ | $\$ 0$ | $\$ 3$ |
| T-50 | $\$ 2$ | $\$ 3$ | $\$ 0$ |

## Step 1

- Check whether we can assign a typesetter to a certain job. See the cell with value " 0 ".

| Typesetter | A |
| :--- | :--- |
| Job | $\$ 5$ |
| R-34 | $\$ 5$ |
| S-66 | $\$ 0$ |
| T-50 | $\$$ |

B cannot assigned to $S$-66 since it has been assigned to
A. Therefore, additional procedure need to be done.

## Step 2 and 3

Step 2 - Lines


Because only two lines are needed to cover all the zeros, the solution is not optimal

The smallest uncovered number is 2 so this is subtracted from all other uncovered numbers and added to numbers at the intersection of lines

Step 3 - Subtraction

| Typesetter | A | B | C |
| :--- | :---: | :---: | :---: |
| Job |  |  |  |
| R-34 | $\$ 3$ | $\$ 4$ | $\$ 0$ |
| S-66 | $\$ 0$ | $\$ 0$ | $\$ 5$ |
| $T-50$ | $\$ 0$ | $\$ 1$ | $\$ 0$ |

## Step 4

Step 2 - Lines


Because three lines are needed, the solution is optimal and assignments can be made

Start by assigning R-34 to worker C as this is the only possible assignment for worker C.

Job T-50 must go to worker A as worker C is already assigned. This leaves S-66 for worker B.

Step 4 - Assignments

| Typesetter | A | B | C |
| :--- | :---: | :---: | :---: |
| Job |  |  |  |
| R-34 | $\$ 3$ | $\$ 4$ | $\$ 0$ |
| S-66 | $\$ 0$ | $\$ 0$ | $\$ 5$ |
| T-50 | $\$ 0$ | $\$ 1$ | $\$ 0$ |

## Optimal

Step 4 - Assignments

| Typesetter | A | B | C |
| :--- | :--- | :--- | :--- |
| Job |  |  |  |
| R-34 | $\$ 11$ | $\$ 14$ | $\$ 6$ |
| S-66 | $\$ 8$ | $\$ 10$ | $\$ 11$ |
| T-50 | $\$ 9$ | $\$ 12$ | $\$ 7$ |


| Typesetter | A | B | C |
| :--- | :--- | :--- | :--- |
| Job |  |  |  |
| S-64 | $\$ 3$ | $\$ 4$ | $\$ 0$ |
| $T-50$ | $\$ 0$ | $\$ 0$ | $\$ 5$ |

From the original cost table
Minimum cost

$$
=\$ 6+\$ 10+\$ 9=\$ 25
$$

## MAXIMIZATION

## Example

## $\boxtimes$ Build a table of efficiencies of British in Patrol Sectors

| SHIP | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| 1 | 20 | 60 | 50 | 55 |
| 2 | 60 | 30 | 80 | 75 |
| 3 | 80 | 100 | 90 | 80 |
| 4 | 65 | 80 | 75 | 70 |

Identify the highest rating score

## Example

## V Compute opportunity costs of British Ships

Subtract each rating from the maximum rating score

| SHIP | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
|  | 80 | 40 | 50 | 45 |
| 2 | 40 | 70 | 20 | 25 |
| 3 | 20 | 0 | 10 | 20 |
| 4 | 35 | 20 | 25 | 30 |
| $=100-20$ |  |  |  |  |

## Step 1

| SHIP | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| 1 | 80 | 40 | 50 | 45 |
| 2 | 40 | 70 | 20 | 25 |
| 3 | 20 | 0 | 10 | 20 |
| 4 | 35 | 20 | 25 | 30 |

Step 1a-Rows

| SHIP | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| 1 | 40 | 0 | 10 | 5 |
| 2 | 20 | 50 | 0 | 5 |
| 3 | 20 | 0 | 10 | 20 |
| 4 | 15 | 0 | 5 | 10 |

Step 1b-Columns

| SHIP | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| 1 | 25 | 0 | 10 | 0 |
| 2 | 5 | 50 | 0 | 0 |
| 3 | 5 | 0 | 10 | 15 |
| 4 | 0 | 0 | 5 | 5 |

## Step 1

- Check whether we can assign a ship to a certain sector. See the cell with value " 0 ".



## Optimal

Step 4 - Assignments

|  | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| SHIP | A | B | C | $\mathbf{D}$ |
| $\mathbf{1}$ | 20 | 60 | 50 | 55 |
| $\mathbf{2}$ | 60 | 30 | 80 | 75 |
| $\mathbf{3}$ | 80 | 100 | 90 | 80 |
| $\mathbf{4}$ | 65 | 80 | 75 | 70 |


|  | SECTOR |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| SHIP | A | B | C | D |
| $\mathbf{1}$ | 25 | 0 | 10 | 0 |
| $\mathbf{2}$ | 5 | 50 | 0 | 0 |
| $\mathbf{3}$ | 5 | 0 | 10 | 15 |
| $\mathbf{4}$ | 0 | 0 | 5 | 5 |

From the original cost table
Maximum efficiencies

$$
=65+100+80+55=300
$$

EXERCISE

## 9-37

In a job shop operation, four jobs may be performed on any of four machines. The hours required for each job on each machine are presented in the following table. The plant supervisor would like to assign jobs so that total time is minimized. Find the best solution.

| JOB | MACHINE |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | W | X | Y | Z |
| A12 | 10 | 14 | 16 | 13 |
| A15 | 12 | 13 | 15 | 12 |
| B2 | 9 | 12 | 12 | 11 |
| B9 | 14 | 16 | 18 | 16 |

## 9-41(1)

Roscoe Davis, chairman of a college's business department, has decided to apply a new method in assigning professors to courses next semester. As a criterion for judging who should teach each course, Professor Davis reviews the past two years' teaching evaluations (which were filled out by students). Since each of the four professors taught each of the four courses at one time or another during the two-year period, Davis is able to record a course rating for each instructor.

## 9-41(2)

These ratings are shown in the table. Find the best assignment of professors to courses to maximize the overall teaching rating.

## COURSE

PROFESSOR STATISTICS MANAGEMENT FINANCE ECONOMICS

| Anderson | 90 | 65 | 95 | 40 |
| :--- | :--- | :--- | :--- | :--- |
| Sweeney | 70 | 60 | 80 | 75 |
| Williams | 85 | 40 | 80 | 60 |
| McKinney | 55 | 80 | 65 | 55 |

## 9-48 (1)

The XYZ Corporation is expanding its market to include Texas. Each salesperson is assigned to potential distributors in one of five different areas. It is anticipated that the salesperson will spend about three to four weeks in each area. A statewide marketing campaign will begin once the product has been delivered to the distributors.

## 9-48 (2)

The five sales people who will be assigned to these areas (one person for each area) have rated the areas on the desirability of the assignment as shown in the following table. The scale is 1 (least desirable) to 5 (most desirable). Which assignments should be made if the total of the ratings is to be maximized?

## 9-48 (3)

|  |  |  |  |  | CORPUS |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | AUSTIN/ |  | EL PASO/ |  | CHRISTI/ |

## TAKE HOME TEST

## Take Home Test

- Buka companion website untuk buku: Quantitative Analysis for Management, 11 ${ }^{\text {th }}$ ed. (Link lihat di blog)
- Buka Internet Homework Problem chapter 7 dan chapter 9.
- Chapter 7: Pilih dan selesaikan 1 soal dengan menggunakan metode grafik dan 1 soal dengan metode simpleks.
- Chapter 9: Pilih dan selesaikan 1 soal model transportasi (initial solution dan optimization) dan 1 soal model penugasan (assigment model).


## THANK YOU

